

Tasks

- 了解back-propagation (BP) 原理
 - 公式推導 → (重點：chain-rule)
 - Error → softmax → sigmod/relu → ... → input
- 更改MNIST for ML Beginners → MLP/DNN
 - 最佳化 → 正確率大於99%
 - Training data + Noises (optinal)
- GPU (optional)
 - NVIDIA CUDA
 - Tensorflow with GPU support
 - 速度改善多少？

Chain Rule

Chain Rule.

Case 1.

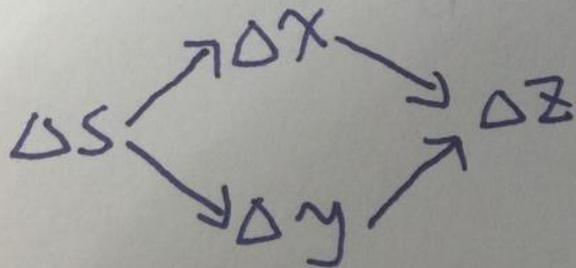
$$y = g(x) \quad z = h(x).$$

$$\Delta x \rightarrow \Delta y \rightarrow \Delta z$$

$$\frac{dz}{dx} = \frac{dz}{dy} \frac{dy}{dx}.$$

Case 2.

$$x = g(s) \quad y = h(s) \quad z = k(x, y)$$



$$\frac{\partial z}{\partial s} = \frac{\partial z}{\partial x} \frac{\partial x}{\partial s} + \frac{\partial z}{\partial y} \frac{\partial y}{\partial s}.$$

Forward Pass

$\frac{\partial C^r}{\partial w_{ij}^l}$ - Forward pass.

Layer $l-1$ Layer l .

Nodes in Layer $l-1$: 1, 2, ..., j .
 Nodes in Layer l : 1, 2, ..., i .

Weight between node j in Layer $l-1$ and node i in Layer l : w_{ij}^l .

Input to node i in Layer l : z_i^l .
 Output of node i in Layer l : a_i^l .

$\Delta w_{ij}^l \rightarrow \Delta z_i^l \rightarrow \Delta C^r$

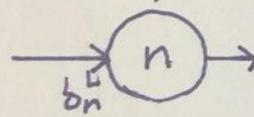
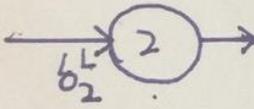
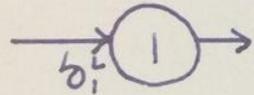
$$\frac{\partial C^r}{\partial w_{ij}^l} = \frac{\partial z_i^l}{\partial w_{ij}^l} \frac{\partial C^r}{\partial z_i^l}$$

if $l > 1$

$$z_i^l = \sum_j w_{ij}^l a_j^{l-1} + b_i^l$$

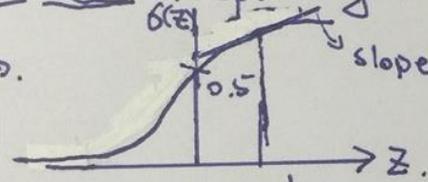
Backward Pass(1)

$\frac{\partial C^r}{\partial z_n^l} \rightarrow \delta_n^l$ 1. How to compute δ^l - Backward pass.
 2. The relation of δ^l and δ^{l+1} .



1. $\delta_n^l = \frac{\partial C^r}{\partial z_n^l} \rightarrow \Delta z_n^l \rightarrow \Delta a_n^l = \Delta y_n^r \rightarrow \Delta C^r$
network output.

$= \frac{\partial y_n^r}{\partial z_n^l} \frac{\partial C^r}{\partial y_n^r}$ → Depending on the definition of cost function.
slope.



$= \sigma'(z_n^l) \frac{\partial C^r}{\partial y_n^r}$
 $\nabla C^r(y^r) = \begin{bmatrix} \frac{\partial C^r}{\partial y_1^r} \\ \frac{\partial C^r}{\partial y_2^r} \\ \vdots \\ \frac{\partial C^r}{\partial y_n^r} \end{bmatrix}$

$\Rightarrow \delta^l = \sigma'(z^l) \cdot \nabla C^r(y^r)$

$\sigma'(z^l) = \begin{bmatrix} \sigma'(z_1^l) \\ \sigma'(z_2^l) \\ \vdots \\ \sigma'(z_n^l) \end{bmatrix}$

Backward Pass(2)

2. $b_i^l = \frac{\partial C^r}{\partial z_i^l}$

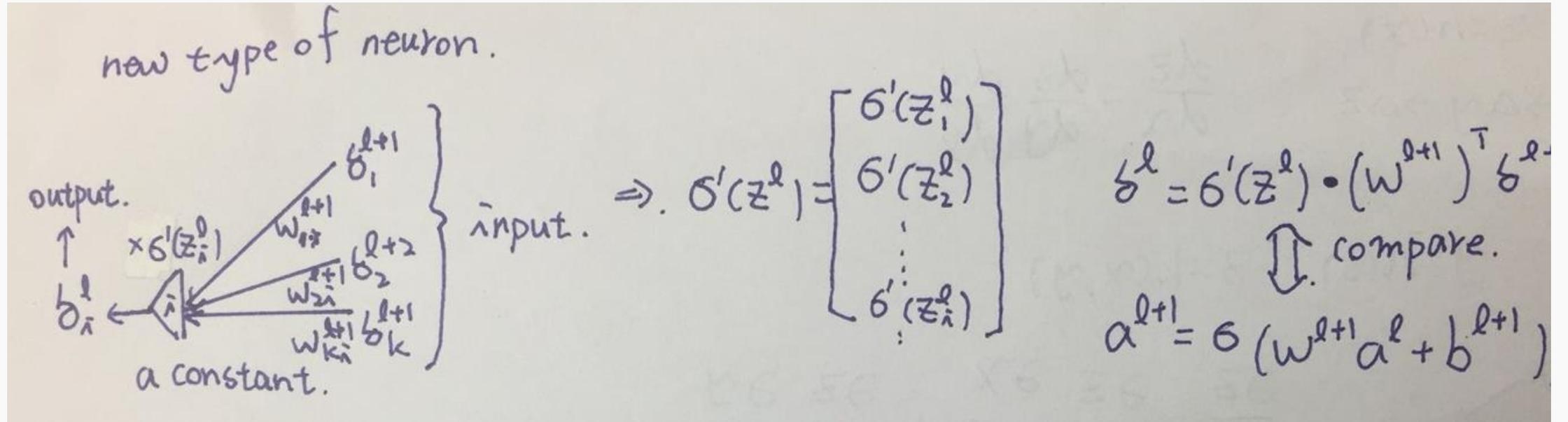
$\Delta z_i^l \rightarrow \Delta a_i^l \rightarrow \begin{cases} \Delta z_1^{l+1} \\ \Delta z_2^{l+1} \\ \Delta z_k^{l+1} \end{cases} \rightarrow \Delta C^r$

$b_i^l = \frac{\partial C^r}{\partial z_i^l} = \frac{\partial a_i^l}{\partial z_i^l} \sum_k \frac{\partial z_k^{l+1}}{\partial a_i^l} \left[\frac{\partial C^r}{\partial z_k^{l+1}} \right] b_k^{l+1} \Rightarrow z_k^{l+1} = \sum_n w_{ki}^{l+1} a_n^l + b_k^{l+1}$

\downarrow
 $\sigma'(z_i^l)$

$\Rightarrow b_i^l = \sigma'(z_i^l) \sum_k w_{ki}^{l+1} b_k^{l+1}$

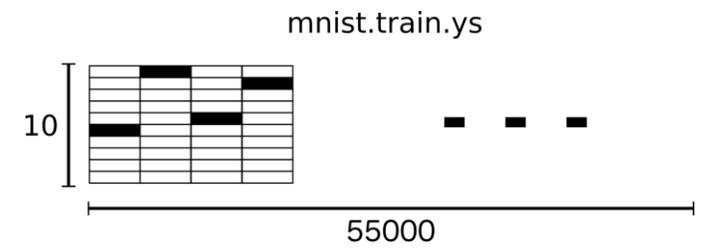
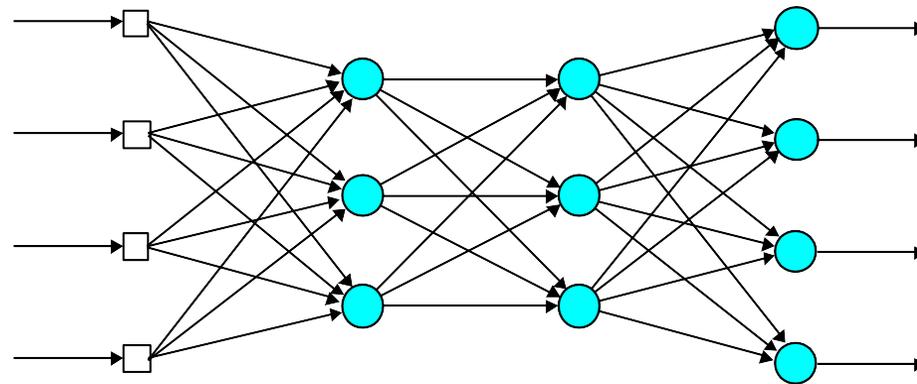
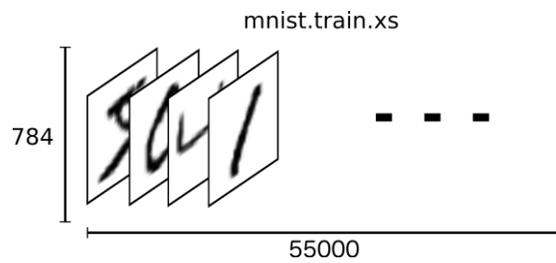
Backward Pass(3)



DNN 訓練流程

- 初始化權重
- 利用目前的權重計算輸出結果
- 計算輸出結果和目標結果的誤差
- 調整權重
- **LOOP STEP2-5**直到收斂

Tensorflow Tutorial



Hidden layer with ReLU&ReLU6

```

# Import data
from tensorflow.examples.tutorials.mnist import input_data

import tensorflow as tf

flags = tf.app.flags
FLAGS = flags.FLAGS
flags.DEFINE_string('data_dir', '/tmp/data/', 'Directory for storing data')

mnist = input_data.read_data_sets(FLAGS.data_dir, one_hot=True)

sess = tf.InteractiveSession()

# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W = tf.Variable(tf.zeros([784, 10]))
b = tf.Variable(tf.zeros([10]))
y = tf.nn.softmax(tf.matmul(x, W) + b)

# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=[1]))
train_step = tf.train.GradientDescentOptimizer(0.5).minimize(cross_entropy)

# Train
tf.initialize_all_variables().run()
for i in range(1000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    train_step.run({x: batch_xs, y_: batch_ys})

# Test trained model
correct_prediction = tf.equal(tf.argmax(y, 1), tf.argmax(y_, 1))
accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
print(accuracy.eval({x: mnist.test.images, y_: mnist.test.labels}))

Extracting /tmp/data/train-images-idx3-ubyte.gz
Extracting /tmp/data/train-labels-idx1-ubyte.gz
Extracting /tmp/data/t10k-images-idx3-ubyte.gz
Extracting /tmp/data/t10k-labels-idx1-ubyte.gz
0.917
    
```

Without Hidden Layer

Performance:0.917

One Hidden Layer

Performance:0.9831

```
host:8888/notebooks/Untitled.ipynb
jupyter Untitled Last Checkpoint: Last Monday at 10:06 PM (autosaved)
File Edit View Insert Cell Kernel Widgets Help Python [conda root]
Code CellToolbar
# Import data
from tensorflow.examples.tutorials.mnist import input_data

import tensorflow as tf

flags = tf.app.flags
FLAGS = flags.FLAGS
flags.DEFINE_string('data_dir', '/tmp/data/', 'Directory for storing data')

mnist = input_data.read_data_sets(FLAGS.data_dir, one_hot=True)

sess = tf.InteractiveSession()

# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W1 = tf.Variable(tf.random_normal([784, 900], stddev=0.01))
b1 = tf.Variable(tf.random_normal([900], stddev=0.01))
x2 = tf.nn.relu(tf.matmul(x, W1) + b1)
W2 = tf.Variable(tf.random_normal([900, 10], stddev=0.01))
b2 = tf.Variable(tf.random_normal([10], stddev=0.01))
y = tf.nn.softmax(tf.matmul(x2, W2) + b2)

# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=[1]))
train_step = tf.train.GradientDescentOptimizer(0.5).minimize(cross_entropy)

# Train
tf.initialize_all_variables().run()
for i in range(10000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    train_step.run({x: batch_xs, y_: batch_ys})

# Test trained model
correct_prediction = tf.equal(tf.argmax(y, 1), tf.argmax(y_, 1))
accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
print(accuracy.eval({x: mnist.test.images, y_: mnist.test.labels}))

Extracting /tmp/data/train-images-idx3-ubyte.gz
Extracting /tmp/data/train-labels-idx1-ubyte.gz
Extracting /tmp/data/t10k-images-idx3-ubyte.gz
Extracting /tmp/data/t10k-labels-idx1-ubyte.gz
0.9831
```

One Hidden Layer (With ReLU6)

```
# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W1 = tf.Variable(tf.random_normal([784, 441], stddev=0.01))
b1 = tf.Variable(tf.random_normal([441], stddev=0.01))
x2 = tf.nn.relu6(tf.matmul(x, W1) + b1)
W2 = tf.Variable(tf.random_normal([441, 10], stddev=0.01))
b2 = tf.Variable(tf.random_normal([10], stddev=0.01))
y = tf.nn.softmax(tf.matmul(x2, W2) + b2)

# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=[1]))
train_step = tf.train.GradientDescentOptimizer(0.5).minimize(cross_entropy)

# Train
tf.initialize_all_variables().run()
for i in range(10000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    train_step.run({x: batch_xs, y_: batch_ys})

# Test trained model
correct_prediction = tf.equal(tf.argmax(y, 1), tf.argmax(y_, 1))
accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
print(accuracy.eval({x: mnist.test.images, y_: mnist.test.labels}))
```

```
Extracting /tmp/data/train-images-idx3-ubyte.gz
Extracting /tmp/data/train-labels-idx1-ubyte.gz
Extracting /tmp/data/t10k-images-idx3-ubyte.gz
Extracting /tmp/data/t10k-labels-idx1-ubyte.gz
0.9817
```

Performance:0.9817

Two Hidden Layer (With ReLU6)

Performance: **0.985**

```
import tensorflow as tf

flags = tf.app.flags
FLAGS = flags.FLAGS
flags.DEFINE_string('data_dir', '/tmp/data/', 'Directory for storing data')

mnist = input_data.read_data_sets(FLAGS.data_dir, one_hot=True)

sess = tf.InteractiveSession()

# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W1 = tf.Variable(tf.random_normal([784, 625], stddev=0.01))
b1 = tf.Variable(tf.random_normal([625], stddev=0.01))
x2 = tf.nn.relu6(tf.matmul(x, W1) + b1)
W2 = tf.Variable(tf.random_normal([625, 441], stddev=0.01))
b2 = tf.Variable(tf.random_normal([441], stddev=0.01))
x3 = tf.nn.relu6(tf.matmul(x2, W2) + b2)
W3 = tf.Variable(tf.random_normal([441, 10], stddev=0.01))
b3 = tf.Variable(tf.random_normal([10], stddev=0.01))
y = tf.nn.softmax(tf.matmul(x3, W3) + b3)

# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=[1]))
train_step = tf.train.GradientDescentOptimizer(0.5).minimize(cross_entropy)

# Train
tf.initialize_all_variables().run()
for i in range(10000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    train_step.run({x: batch_xs, y_: batch_ys})

# Test trained model
correct_prediction = tf.equal(tf.argmax(y, 1), tf.argmax(y_, 1))
accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
print(accuracy.eval({x: mnist.test.images, y_: mnist.test.labels}))

Extracting /tmp/data/train-images-idx3-ubyte.gz
Extracting /tmp/data/train-labels-idx1-ubyte.gz
Extracting /tmp/data/t10k-images-idx3-ubyte.gz
Extracting /tmp/data/t10k-labels-idx1-ubyte.gz
0.985
```

Three Hidden Layer (With ReLU6)

Performance:0.9847

```
# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W1 = tf.Variable(tf.random_normal([784, 612], stddev=0.01))
b1 = tf.Variable(tf.random_normal([612], stddev=0.01))
x2 = tf.nn.relu6(tf.matmul(x, W1) + b1)
W2 = tf.Variable(tf.random_normal([612, 466], stddev=0.01))
b2 = tf.Variable(tf.random_normal([466], stddev=0.01))
x3 = tf.nn.relu6(tf.matmul(x2, W2) + b2)
W3 = tf.Variable(tf.random_normal([466, 211], stddev=0.01))
b3 = tf.Variable(tf.random_normal([211], stddev=0.01))
x4 = tf.nn.relu6(tf.matmul(x3, W3) + b3)
W4 = tf.Variable(tf.random_normal([211, 10], stddev=0.01))
b4 = tf.Variable(tf.random_normal([10], stddev=0.01))
y = tf.nn.softmax(tf.matmul(x4, W4) + b4)

# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=
train_step = tf.train.GradientDescentOptimizer(0.5).minimize(cross_entropy)

# Train
tf.initialize_all_variables().run()
for i in range(10000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    train_step.run({x: batch_xs, y_: batch_ys})

# Test trained model
correct_prediction = tf.equal(tf.argmax(y, 1), tf.argmax(y_, 1))
accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
print(accuracy.eval({x: mnist.test.images, y_: mnist.test.labels}))
```

```
Extracting /tmp/data/train-images-idx3-ubyte.gz
Extracting /tmp/data/train-labels-idx1-ubyte.gz
Extracting /tmp/data/t10k-images-idx3-ubyte.gz
Extracting /tmp/data/t10k-labels-idx1-ubyte.gz
0.9847
```

Four Hidden Layer (With ReLU6) 10000 epoch

Performance:0.982

```
# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W1 = tf.Variable(tf.random_normal([784, 629],stddev=0.01))
b1 = tf.Variable(tf.random_normal([629],stddev=0.01))
x2 = tf.nn.relu6(tf.matmul(x, W1) + b1)
W2 = tf.Variable(tf.random_normal([629, 474],stddev=0.01))
b2 = tf.Variable(tf.random_normal([474],stddev=0.01))
x3 = tf.nn.relu6(tf.matmul(x2, W2) + b2)
W3 = tf.Variable(tf.random_normal([474, 319],stddev=0.01))
b3 = tf.Variable(tf.random_normal([319],stddev=0.01))
x4 = tf.nn.relu6(tf.matmul(x3, W3) + b3)
W4 = tf.Variable(tf.random_normal([319, 164],stddev=0.01))
b4 = tf.Variable(tf.random_normal([164],stddev=0.01))
x5 = tf.nn.relu6(tf.matmul(x4, W4) + b4)
W5 = tf.Variable(tf.random_normal([164, 10],stddev=0.01))
b5 = tf.Variable(tf.random_normal([10],stddev=0.01))
y = tf.nn.softmax(tf.matmul(x5, W5) + b5)

# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=[1]))
train_step = tf.train.GradientDescentOptimizer(0.5).minimize(cross_entropy)

# Train
tf.initialize_all_variables().run()
for i in range(10000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    train_step.run({x: batch_xs, y_: batch_ys})

# Test trained model
correct_prediction = tf.equal(tf.argmax(y, 1), tf.argmax(y_, 1))
accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
print(accuracy.eval({x: mnist.test.images, y_: mnist.test.labels}))
```

```
Extracting /tmp/data/train-images-idx3-ubyte.gz
Extracting /tmp/data/train-labels-idx1-ubyte.gz
Extracting /tmp/data/t10k-images-idx3-ubyte.gz
Extracting /tmp/data/t10k-labels-idx1-ubyte.gz
0.9824
```

Four Hidden Layer (With ReLU6) 5000 epoch

Performance:0.9772

```
# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W1 = tf.Variable(tf.random_normal([784, 629], stddev=0.01))
b1 = tf.Variable(tf.random_normal([629], stddev=0.01))
x2 = tf.nn.relu6(tf.matmul(x, W1) + b1)
W2 = tf.Variable(tf.random_normal([629, 474], stddev=0.01))
b2 = tf.Variable(tf.random_normal([474], stddev=0.01))
x3 = tf.nn.relu6(tf.matmul(x2, W2) + b2)
W3 = tf.Variable(tf.random_normal([474, 319], stddev=0.01))
b3 = tf.Variable(tf.random_normal([319], stddev=0.01))
x4 = tf.nn.relu6(tf.matmul(x3, W3) + b3)
W4 = tf.Variable(tf.random_normal([319, 164], stddev=0.01))
b4 = tf.Variable(tf.random_normal([164], stddev=0.01))
x5 = tf.nn.relu6(tf.matmul(x4, W4) + b4)
W5 = tf.Variable(tf.random_normal([164, 10], stddev=0.01))
b5 = tf.Variable(tf.random_normal([10], stddev=0.01))
y = tf.nn.softmax(tf.matmul(x5, W5) + b5)

# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=[1]))
train_step = tf.train.GradientDescentOptimizer(0.5).minimize(cross_entropy)

# Train
tf.initialize_all_variables().run()
for i in range(5000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    train_step.run({x: batch_xs, y_: batch_ys})

# Test trained model
correct_prediction = tf.equal(tf.argmax(y, 1), tf.argmax(y_, 1))
accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
print(accuracy.eval({x: mnist.test.images, y_: mnist.test.labels}))
```

```
Extracting /tmp/data/train-images-idx3-ubyte.gz
Extracting /tmp/data/train-labels-idx1-ubyte.gz
Extracting /tmp/data/t10k-images-idx3-ubyte.gz
Extracting /tmp/data/t10k-labels-idx1-ubyte.gz
0.9772
```

Hidden layer with Sigmoid

Two Hidden Layer

Performance:0.9653

```
# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W1 = tf.Variable(tf.random_normal([784, 516],stddev=0.01))
b1 = tf.Variable(tf.random_normal([516],stddev=0.01))
x2 = tf.nn.sigmoid(tf.matmul(x, W1) + b1)
W2 = tf.Variable(tf.random_normal([516, 258],stddev=0.01))
b2 = tf.Variable(tf.random_normal([258],stddev=0.01))
x3 = tf.nn.sigmoid(tf.matmul(x2, W2) + b2)
W3 = tf.Variable(tf.random_normal([258, 10],stddev=0.01))
b3 = tf.Variable(tf.random_normal([10],stddev=0.01))
y = tf.nn.softmax(tf.matmul(x3, W3) + b3)

# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=[1]))
train_step = tf.train.GradientDescentOptimizer(0.5).minimize(cross_entropy)

# Train
tf.initialize_all_variables().run()
for i in range(10000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    train_step.run({x: batch_xs, y_: batch_ys})

# Test trained model
correct_prediction = tf.equal(tf.argmax(y, 1), tf.argmax(y_, 1))
accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
print(accuracy.eval({x: mnist.test.images, y_: mnist.test.labels}))
```

```
Extracting /tmp/data/train-images-idx3-ubyte.gz
Extracting /tmp/data/train-labels-idx1-ubyte.gz
Extracting /tmp/data/t10k-images-idx3-ubyte.gz
Extracting /tmp/data/t10k-labels-idx1-ubyte.gz
0.9653
```

Three Hidden Layer

Performance:0.9432

```
# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W1 = tf.Variable(tf.random_normal([784, 580],stddev=0.01))
b1 = tf.Variable(tf.random_normal([580],stddev=0.01))
x2 = tf.nn.sigmoid(tf.matmul(x, W1) + b1)
W2 = tf.Variable(tf.random_normal([580, 386],stddev=0.01))
b2 = tf.Variable(tf.random_normal([386],stddev=0.01))
x3 = tf.nn.sigmoid(tf.matmul(x2, W2) + b2)
W3 = tf.Variable(tf.random_normal([386, 192],stddev=0.01))
b3 = tf.Variable(tf.random_normal([192],stddev=0.01))
x4 = tf.nn.sigmoid(tf.matmul(x3, W3) + b3)
W4 = tf.Variable(tf.random_normal([192, 10],stddev=0.01))
b4 = tf.Variable(tf.random_normal([10],stddev=0.01))
y = tf.nn.softmax(tf.matmul(x4, W4) + b4)

# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=[1]))
train_step = tf.train.GradientDescentOptimizer(0.5).minimize(cross_entropy)

# Train
tf.initialize_all_variables().run()
for i in range(10000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    train_step.run({x: batch_xs, y_: batch_ys})

# Test trained model
correct_prediction = tf.equal(tf.argmax(y, 1), tf.argmax(y_, 1))
accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
print(accuracy.eval({x: mnist.test.images, y_: mnist.test.labels}))
```

```
Extracting /tmp/data/train-images-idx3-ubyte.gz
Extracting /tmp/data/train-labels-idx1-ubyte.gz
Extracting /tmp/data/t10k-images-idx3-ubyte.gz
Extracting /tmp/data/t10k-labels-idx1-ubyte.gz
0.9432
```

Hidden layer with Dropout

Two Hidden Layer (With ReLU6)

Performance:0.9472

```
# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W1 = tf.Variable(tf.random_normal([784, 516], stddev=0.01))
b1 = tf.Variable(tf.random_normal([516], stddev=0.01))
x2 = tf.nn.dropout(tf.nn.relu6(tf.matmul(x, W1) + b1), 0.33)
W2 = tf.Variable(tf.random_normal([516, 258], stddev=0.01))
b2 = tf.Variable(tf.random_normal([258], stddev=0.01))
x3 = tf.nn.dropout(tf.nn.relu6(tf.matmul(x2, W2) + b2), 0.33)
W3 = tf.Variable(tf.random_normal([258, 10], stddev=0.01))
b3 = tf.Variable(tf.random_normal([10], stddev=0.01))
y = tf.nn.softmax(tf.matmul(x3, W3) + b3)

# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=[1]))
train_step = tf.train.GradientDescentOptimizer(0.03).minimize(cross_entropy)

# Train
tf.initialize_all_variables().run()
for i in range(10000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    train_step.run({x: batch_xs, y_: batch_ys})

# Test trained model
correct_prediction = tf.equal(tf.argmax(y, 1), tf.argmax(y_, 1))
accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
print(accuracy.eval({x: mnist.test.images, y_: mnist.test.labels}))
```

```
Extracting /tmp/data/train-images-idx3-ubyte.gz
Extracting /tmp/data/train-labels-idx1-ubyte.gz
Extracting /tmp/data/t10k-images-idx3-ubyte.gz
Extracting /tmp/data/t10k-labels-idx1-ubyte.gz
0.9472
```

Result

Model	Result
Without Hidden Layer	0.917
One Hidden Layer	0.9831
One Hidden Layer(With ReLU6)	0.9817
Two Hidden Layer(With ReLU6)	0.985
Three Hidden Layer(With ReLU6)	0.9847
Four Hidden Layer(With ReLU6)10000 epoch	0.982
Four Hidden Layer(With ReLU6)5000 epoch	0.9772
Two Hidden Layer(Sigmoid)	0.9653
Three Hidden Layer(Sigmoid)	0.9432
Two Hidden Layer(Dropout with ReLU6)	0.9472

Thanks